

Merry-Go-Round Example

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- A merry go round of mass M and radius R rotates freely about a frictionless vertical axle. A student with mass m walks from the rim of the disk to the center. If the angular speed of the system is ω when the student is at the rim, what is the angular speed when the student is halfway to the center ($R/2$)?

Initial moment of inertia I_i

$$\begin{aligned} I_i &= I_{mi} + I_{si} \\ &= \underset{\substack{\uparrow \\ \text{rotating} \\ \text{disk}}}{\frac{1}{2}MR^2} + \underset{\substack{\uparrow \\ \text{point mass}}}{mR^2} \end{aligned}$$

$$\begin{aligned} I_f &= I_{mf} + I_{sf} \\ &= \frac{1}{2}MR^2 + mr^2 \end{aligned}$$

Angular momentum is conserved

$$\begin{aligned} I_i \omega_i &= I_f \omega_f \\ \left(\frac{1}{2}MR^2 + mR^2\right) \omega_i &= \left(\frac{1}{2}MR^2 + mr^2\right) \omega_f \\ \omega_f &= \frac{\left(\frac{1}{2}MR^2 + mR^2\right) \omega_i}{\left(\frac{1}{2}MR^2 + m(R/2)^2\right)} \end{aligned}$$